South Pacific Regional Fisheries Management Organisation

2nd Meeting of the Scientific Committee

Honolulu, Hawaii, USA 1-7 October 2014

SC-02-JM-11

CPUE of Jack mackerel at the center-south area off Chile 1983-2014

Cristian Canales

CPUE of Jack mackerel (*Trachurus murphy*) at the center-south area off Chile 1983-2014.

Cristian Canales (cristian.canales@ifop.cl)

Summary

In this work, the jack mackerel CPUE is updated via a Generalized Lineal Model based on the purse seine information at the center-south area off Chile. The fishing effort is defined as haul capacity displaced by day out of port, and several factors were considered to explain the CPUE variations and the catches success. In this sense, the abundance index is the result of the product between estimators of CPUE and success of catches.

Results show that the population declined steadily until mid 90's. After a transient stability state, since 2006 a faster declination was observed and the stock depletion had reached the lower value equivalent to 12% of the CPUE recorded in 1983. Although a scale change occurred in 2012 due to an increase in the availability/catchability, the population has continued its declining trend until the present.

1. Introduction

The stock assessment of jack mackerel is the most important scientific activity carried out by the Scientific Committee of the South Pacific Regional Fisheries Management Organization (SPRFMO). This activity implies the analysis of several information sets provided by Member States of this organization, such as the Catch per Unit of Effort (CPUE). CPUE is an abundance index that needs to be updated since it gives an important support to stock assessment models in order to precise the population trend, particularly for recent years.

In order to evaluate the CPUE variability, it is necessary to consider an appropriate statistical analysis that allows the exploration of the main factors that determine this variability, such as the year effect, commonly considered as abundance index. In this report, the CPUE modeling work for jack mackerel, corresponding to the purse seine fleet at the center-south area off Chile (Fleet 2) between 1983 and 2014, is informed.

2. Materials and Methods

The fishing logbooks of the purse seine fleet at the center-south area off Chile from 1983 to 2014 were analyzed. The area was divided in 9 sub-zones based on 3 latitudinal strata: 32°10'S - 34°50'S, 34°50'S - 38°00'S, and 38°00'S - 47°00'S, and 3 ranges of distance from the coast: 0-100 nm; 101-200 nm; and >200 nm (Fig. 1). Also, the fleet was composed of 10 groups based on its haul capacity: <250 m3; 250-350 m3; 351-500 m3; 501-600 m3; 601-750 m3; 751-850 m3; 851-910 m3; 911-1.100 m3; 1.101-1.500 m3, and 1.501-2.071 m3, while the intra annual variability was modeled in base of

quarters. The unit of effort corresponds to the haul capacity displaced by days out of port (m3 x dop) and CPUE is the rate between the catch by trip in tons, and the effort unit.

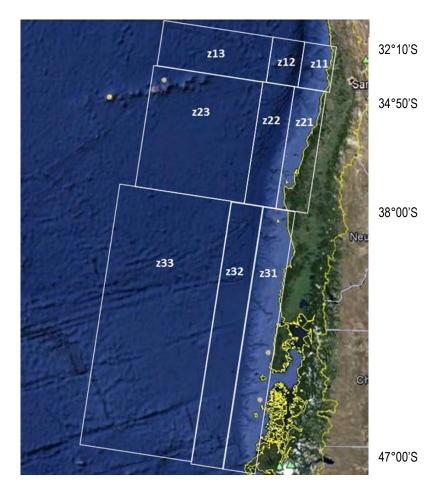


Figure 1. Spatial representation of Jack mackerel fishing zones at the center-south area off Chile.

The CPUE analysis was conducted considering a Lineal Generalized Model (GLM; McCullagh & Nelder, 1989). Following the proposal of Stefánsson (1996), Welsh et al. (1996) and Fletcher et al. (2005), data without catches were analyzed independently from trips with catches following a Delta model where an estimator of expected CPUE value as abundance index corresponds to a mixture of models given by:

$$\begin{array}{l}
+ * \dot{P}_{y} \\
CP\dot{D}E_{y} = CP\dot{D}E_{y}
\end{array} \tag{1}$$

$$+ CPUE_{y,q,cb,z}$$

$$log$$
(2)

$$log\left(\frac{P_{y,q,cb,z}}{1-P_{y,q,cb,z}}\right) = c2 + Y'_{y} + Q'_{q} + CB'_{cb} + Z'_{z} + y_{,q,cb,z}$$
(3)

where $CPUE_y$ is the annual CPUE (y) for days with catch and P_y is the annual proportion of these days, also defined as fishing success. The terms c1 and c2 are constants, Y is the year factor, Q the quarter, CB the haul capacity strata and Z the zone. ε and σ are terms related to observation error. A deviance analysis was conducted to evaluate the significance of each effect and three models were defined:

Table 1.

GLM models applied to jack mackerel data at the center-south area off Chile

| Model | Variable | Family | Link function |
|-------|-----------|----------|---------------|
| 1 | log(CPUE) | Gauss | Identity |
| 2 | CPUE | Gamma | Log |
| 3 | Binary | Binomial | logit |

The estimators of CPUE and catch success in annual base were estimated as:

$$+= exp(c1 + Y_y + 0.5\sigma^2)$$

$$CP\hat{U}E_y$$
(4)

$$\hat{P}_{y} = \frac{exp(c2+Y'_{y})}{1+exp(c2+Y'_{y})}$$
 (5)

3. Results

3.1. Data exploratory analysis

The nominal CPUE showed a steady decline throughout the analyzed period. While the number of trips declined significantly since 1995, the duration of these gradually increased as a result of the expansion of fishing areas (Table 2). The spatial and temporal distribution of fishing effort indicates that together with an increase of catches, fishing effort gradually covers more remote areas far from the coast and, at mid 90's, the fleet had more participation outside the EEZ in south-central Chile (Table 3). This operation outside the EEZ had its peak between 2008 and 2011 with fishing trips over six days as average, a situation that radically changed in the most recent years when the most important fishing areas were within the EEZ and mainly north of 38° S.

In regard to modeling, examination of the data shows a significant correlation between the logarithm of the CPUE average and the logarithm of the variance of the CPUE, in which the slope statistically has a value of two and the intercept a value of zero (p-value <0.025), suggesting that in the GLM a Gamma link function could be considered as initial candidate (Stefánsson, 1996; Brynjarsdóttir & Stefánsson, 2004). (Fig. 2).

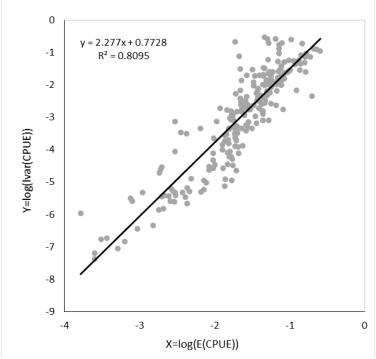


Figure 2. Relationship between log-mean and log-variance of the CPUE of jack mackerel

Table 2.

Summary of information from logbooks and nominal CPUE of jack mackerel at the south-central area off Chile 1983-2014.

| Voor | Total tring | Trips with | Days out port | CPUE (t*m-3/dop) | |
|------|-------------|------------|---------------|------------------|------|
| Year | Total trips | catches | (average) | Mean | max |
| 1983 | 9232 | 6356 | 0.61 | 0.50 | 3.91 |
| 1984 | 8832 | 6051 | 0.63 | 0.46 | 3.85 |
| 1985 | 11998 | 7465 | 0.63 | 0.37 | 4.00 |
| 1986 | 13187 | 8679 | 0.74 | 0.32 | 3.89 |
| 1987 | 12890 | 8834 | 0.72 | 0.40 | 3.99 |
| 1988 | 13399 | 8889 | 0.73 | 0.35 | 3.75 |
| 1989 | 13254 | 9394 | 0.80 | 0.35 | 3.83 |
| 1990 | 15782 | 10284 | 0.85 | 0.28 | 3.90 |
| 1991 | 13208 | 9826 | 1.01 | 0.34 | 3.88 |
| 1992 | 11132 | 7707 | 1.36 | 0.29 | 4.00 |
| 1993 | 10221 | 7240 | 1.60 | 0.26 | 3.69 |
| 1994 | 10232 | 8206 | 1.75 | 0.29 | 3.96 |
| 1995 | 11431 | 9032 | 1.76 | 0.27 | 3.85 |
| 1996 | 7848 | 6379 | 1.96 | 0.27 | 3.90 |
| 1997 | 9655 | 7415 | 1.92 | 0.19 | 3.55 |
| 1998 | 4423 | 3853 | 2.39 | 0.17 | 3.44 |
| 1999 | 2964 | 2676 | 2.41 | 0.17 | 1.71 |
| 2000 | 2737 | 2576 | 2.17 | 0.18 | 1.75 |
| 2001 | 2835 | 2677 | 2.08 | 0.22 | 2.37 |
| 2002 | 2571 | 2348 | 2.83 | 0.18 | 2.91 |
| 2003 | 2196 | 2082 | 3.07 | 0.17 | 2.35 |
| 2004 | 1999 | 1902 | 3.00 | 0.17 | 2.47 |
| 2005 | 1687 | 1606 | 3.28 | 0.16 | 1.84 |
| 2006 | 1434 | 1399 | 3.13 | 0.19 | 2.06 |
| 2007 | 1629 | 1537 | 3.94 | 0.13 | 0.92 |
| 2008 | 996 | 850 | 6.48 | 0.08 | 2.66 |
| 2009 | 1062 | 934 | 6.47 | 0.07 | 3.28 |
| 2010 | 452 | 362 | 7.60 | 0.05 | 0.76 |
| 2011 | 528 | 452 | 6.92 | 0.03 | 0.23 |
| 2012 | 524 | 490 | 3.12 | 0.11 | 0.95 |
| 2013 | 513 | 486 | 3.48 | 0.09 | 0.48 |
| 2014 | 325 | 310 | 3.98 | 0.07 | 0.33 |

Tabla 3.

Representation of fishing effort by year and fishing zone. Bars represent the effort's magnitude.

3.2. Modeling of CPUE and catch success

The CPUE model that considered the Gama link function (Model 2) explained the CPUE variability in a better way than the model of the log-CPUE based on canonical link function (model 1). With the first of these the explanation of the total deviance reached 21% (Table 4). Regardless of the model and while all factors were significant (p-value <0.025), the year effect was the factor with the greatest impact in the explanation of the total deviance (15% -17%), followed far behind by the quarterly effect with less than 3%, and the hold capacity and the fishing area with 1%.

On the other hand, the binomial model applied to the proportion of days with catches shows that the level of explanation of the deviance is low and reaches 12% (Table 4). The year effect was the most important factor but explains only 7% of the total residual deviance. The residual's graph shows that while both models have a symmetric distribution (Fig. 3, 4), in model 2 the overlap of the expected theoretical quantile on the line seems to be higher, ratifying that the best link function in the model is the Gamma function.

The coefficients associated with the year effect are given in Table 5 and 6, highlighting that in general all levels are significant; however, the annual effect of 1983 in model 2 CPUE (Table 5), seems to be not significant. In relation to the other factors in the model, we emphasize that the seasonal effect of the fishery has been well represented by the model, with CPUE being more important in the first two quarters declining rapidly towards the end of the year.

Similarly, the spatial pattern shows that the highest densities of jack mackerel are located north of 38°S and within the EEZ, while in oceanic areas the highest abundances are located south 34°50′S (Fig. 5). Regarding the catch success, the highest values are found between 100 and 200 nm, as well as within the 100 nm but south of 38°S. Historically, the zone between 34°50′S and 38°00′S, outside the EEZ, has the lowest probability of success (52%) (Fig. 6).

The annual effect of GLM for both models of CPUE with catches data does not show major differences in its trends, which are characterized by a significant decline during most of the period of analysis, with the exception of 2012, when the CPUE increased as the result of the operation within the EEZ. Meanwhile, the annual signal of capture success shows three periods: the first from 1983 to 1996 with an average of 70% catch's success; a second period extending from 1997 to 2000 when a sustained increase in catch success occurred; and the third period from 2001 onward with an average of 96% in catch success (on days out of port) (Fig. 7).

Table 4.

Deviance analysis for GLM fitted to the data of jack mackerel fishery. The percentage indicates the proportion of the total deviance explained.

| Model 1 (Gaussian) | | | | | |
|--------------------|-----|----------|------------|-------------|-----|
| Explained deviance | | 19% | | | |
| | d.f | Deviance | d.f. resid | Resid. Dev. | % |
| NULL | | | 147498 | 201973 | |
| Year | 32 | 30553 | 147466 | 171420 | 15% |
| Quart | 3 | 6275 | 147463 | 165146 | 3% |
| Zone | 8 | 1152 | 147455 | 163993 | 1% |
| Hold capacity | 9 | 1051 | 147446 | 162943 | 1% |
| | | | | | |
| Model 2 (Gamma) | | | | | |
| Explained deviance | | 21% | | | |
| | d.f | Deviance | d.f. resid | Resid. Dev. | % |
| NULL | | | 147498 | 158247 | |
| Year | 32 | 27201 | 147466 | 131046 | 17% |
| Quart | 3 | 3050 | 147463 | 127996 | 2% |
| Zone | 8 | 1476 | 147455 | 126520 | 1% |
| Hold capacity | 9 | 1446 | 147446 | 125074 | 1% |
| | | | | | |
| Model 3 (Binomial) | | | | | |
| Explained deviance | | 12% | | | |
| | d.f | Deviance | d.f. resid | Resid. Dev. | % |
| NULL | | | 198199 | 225403 | |
| Year | 32 | 16058 | 198167 | 209345 | 7% |
| Quart | 3 | 3215 | 198164 | 206130 | 1% |
| Zone | 8 | 4904 | 198156 | 201226 | 2% |
| Hold capacity | 9 | 2924 | 198147 | 198301 | 1% |

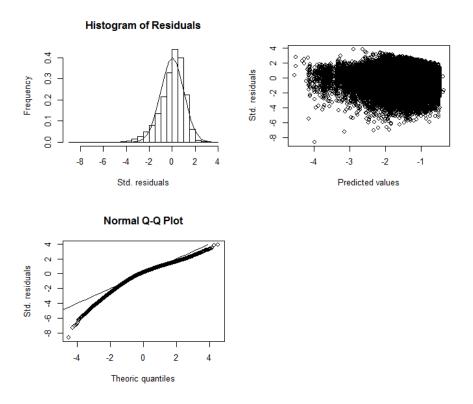


Figure 3. Diagnostic of residuals GLM, CPUE data, Model 1

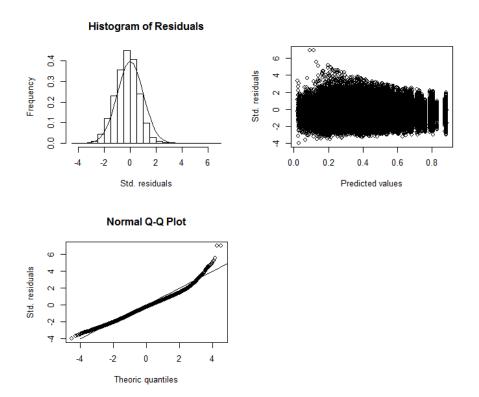


Figure 4. Diagnostic of residuals GLM, CPUE data, Model 2

Table 5.

GLM coefficients (model 2) fitted to positive CPUE data of jack mackerel in central-southern Chile.

```
Estimate Std. Error t value Pr(>|t|)
                      0.035681 -4.042 5.31e-05 ***
(Intercept) -0.144211
vear1983
           -0.006149
                      0.035541
                                -0.173 0.86265
           -0.092706
                      0.035773 -2.591 0.00956 **
vear1984
                      0.035601 -5.986 2.15e-09 ***
year1985
           -0.213118
year1986
           -0.377468
                      0.035478 -10.639 < 2e-16 ***
                      0.035590 -5.682 1.33e-08 ***
year1987
           -0.202221
year1988
           -0.324434
                      0.035787 -9.066 < 2e-16 ***
                      0.035792 -9.479 < 2e-16 ***
year1989
           -0.339263
                                        < 2e-16 ***
year1990
           -0.484148
                      0.035712 -13.557
                      0.035958 -10.359 < 2e-16 ***
year1991
           -0.372510
                      0.036342 -12.151 < 2e-16 ***
year1992
           -0.441597
                      0.036493 -15.039 < 2e-16 ***
0.036516 -12.929 < 2e-16 ***
year1993
           -0.548824
vear1994
           -0.472102
                      0.036593 -15.773 < 2e-16 ***
year1995
           -0.577195
                      0.037014 -15.350 < 2e-16 ***
year1996
           -0.568173
                                        < 2e-16 ***
year1997
           -0.760337
                      0.036715 -20.709
           -0.924414
                      0.038388 -24.081 < 2e-16 ***
vear1998
           year1999
                      0.039883 -23.197 < 2e-16 ***
0.039883 -18.581 < 2e-16 ***
year2000
           -0.925180
year2001
           -0.741079
                                        < 2e-16 ***
year2002
           -0.870051
                      0.041162 -21.137
                                        < 2e-16 ***
year2003
           -0.992971
                      0.041372 -24.001
                                        < 2e-16 ***
           -0.907946
                      0.041706 -21.770
year2004
year2005
           -0.995940
                      0.043102 -23.107
                                        < 2e-16 ***
                      0.043677 -20.729 < 2e-16 ***
year2006
           -0.905405
year2007
           -1.187606
                      0.043972 -27.008 < 2e-16 ***
                      0.049903 -31.094 < 2e-16 ***
year2008
           -1.551652
           -1.734717
                      0.047830 -36.269 < 2e-16 ***
year2009
                      0.061123 -33.134 < 2e-16 ***
year2010
           -2.025250
                                        < 2e-16 ***
           -2.603992
                      0.057129 -45.581
vear2011
                      0.054634 -27.027 < 2e-16 ***
year2012
           -1.476595
           -1.656186
                      0.054864 -30.187 < 2e-16 ***
year2013
           -1.942684
                      0.063925 -30.390 < 2e-16 ***
year2014
                      0.006055 17.053 < 2e-16 ***
trim2
            0.103250
                      0.006606 -9.881 < 2e-16 ***
trim3
           -0.065273
                      0.007763 -49.206 < 2e-16 ***
           -0.382000
trim4
                      0.021724 -5.669 1.44e-08 ***
zona12
           -0.123151
                      0.036805 -12.006 < 2e-16 ***
           -0.441886
zona13
           zona21
                      0.015926 -6.594 4.30e-11 ***
0.025252 -12.077 < 2e-16 ***
           -0.105011
zona22
zona23
           -0.304968
                      0.012176 -28.149 < 2e-16 ***
zona31
           -0.342734
                      0.024506 -13.432 < 2e-16 ***
zona32
           -0.329173
zona33
           -0.379184
                      0.026288 -14.424
                                        < 2e-16 ***
cb2
           -0.006171
                      0.010412 -0.593 0.55341
           -0.060120
                      0.009720 -6.185 6.23e-10 ***
cb3
           -0.209756
                      0.012852 -16.321 < 2e-16 ***
cb4
                                        < 2e-16 ***
cb5
           -0.246076
                      0.011050 -22.269
                      0.015206 -25.692 < 2e-16 ***
           -0.390674
cb6
                                        < 2e-16 ***
                      0.016055 -22.337
cb7
           -0.358613
                                        < 2e-16 ***
                       0.013254 -23.469
cb8
           -0.311057
                      0.013749 -30.860 < 2e-16 ***
           -0.424288
ch9
cb10
           -0.475599
                      0.015783 -30.135 < 2e-16 ***
(Dispersion parameter for Gamma family taken to be 0.80561)
    Null deviance: 158247 on 147498 degrees of freedom
```

Residual deviance: 125074 on 147446 degrees of freedom

Coefficients:

Table 6.

GLM coefficients fitted to the catches success of jack mackerel in central-southern Chile.

```
Coefficients:
           Estimate Std. Error z value Pr(>|z|)
                      0.03682 41.763 < 2e-16 ***
(Intercept) 1.53769
                                      < 2e-16 ***
vear1983
          -0.61403
                       0.03589 -17.107
                      0.03656 -22.496 < 2e-16 ***
           -0.82249
vear1984
                     0.03449 -33.431 < 2e-16 ***
year1985
           -1.15313
year1986
           -1.08957
                      0.03453 -31.557
                                      < 2e-16 ***
                      0.03528 -29.954 < 2e-16 ***
year1987
           -1.05679
year1988
           -1.24825
                      0.03542 -35.244 < 2e-16 ***
           -1.11699
                      0.03632 -30.756 < 2e-16 ***
year1989
year1990
           -1.38524
                      0.03530 -39.247 < 2e-16 ***
           -1.05707
                      0.03750 -28.191 < 2e-16 ***
year1991
                     0.03820 -36.313 < 2e-16 ***
year1992
           -1.38706
           -1.44869
                      0.03934 -36.824 < 2e-16 ***
vear1993
                      0.04213 -26.940 < 2e-16 ***
year1994
           -1.13506
year1995
           -1.17483
                     0.04154 -28.280 < 2e-16 ***
           -1.07284
                     0.04603 -23.310 < 2e-16 ***
year1996
year1997
           -0.77225
                      0.04660 -16.572 < 2e-16 ***
           -0.33050
                     0.07122 -4.641 3.48e-06 ***
vear1998
                               6.200 5.63e-10 ***
year1999
           4.39174
                     0.70829
year2000
           0.51475
                      0.10866
                                4.737 2.17e-06 ***
                                8.450 < 2e-16 ***
year2001
            2.47039
                      0.29234
                                6.653 2.86e-11 ***
year2002
           3.35121
                      0.50368
                                9.082 < 2e-16 ***
year2003
           4.60149
                      0.50665
            5.55945
                      0.99709
                                5.576 2.47e-08 ***
year2004
                                5.460 4.77e-08 ***
year2005
           5.46141
                      1.00033
                                5.637 1.73e-08 ***
year2006
           4.01709
                     0.71262
                      0.31273 11.307 < 2e-16 ***
year2007
            3.53605
                                8.015 1.10e-15 ***
year2008
            2.97988
                      0.37180
                                6.950 3.67e-12 ***
           2.77336
year2009
                     0.39907
year2010
           1.99070
                     0.48139
                                4.135 3.55e-05 ***
            1.14610
                      0.40913
                                2.801 0.005090 **
vear2011
           2.95885
                               2.950 0.003182 **
year2012
                      1.00313
year2013
           -0.44713
                     0.20902 -2.139 0.032423 *
                      0.29009 -1.168 0.242770
0.01486 2.918 0.003517 **
year2014
           -0.33885
trim2
           0.04336
                     0.01488 -28.677 < 2e-16 ***
trim3
           -0.42676
                     0.01576 -54.378 < 2e-16 ***
           -0.85707
trim4
                      0.09504 13.909 < 2e-16 ***
zona12
            1.32190
                     0.14336 -6.348 2.18e-10 ***
zona13
           -0.91009
                               3.600 0.000318 ***
zona21
           0.08071 0.02242
            1.47818
                      0.06958 21.245 < 2e-16 ***
zona22
                      0.06853 -35.633 < 2e-16 ***
zona23
           -2.44211
                     0.04050 25.990 < 2e-16 ***
zona31
           1.05252
            2.11085
                      0.21493
                                9.821 < 2e-16 ***
zona32
                                0.134 0.893137
zona33
            0.05815
                      0.43285
                               20.195 < 2e-16 ***
cb2
            0.37892
                      0.01876
            0.58653
                       0.01791
                               32.739 < 2e-16 ***
cb3
            0.79996
                      0.02606
                                30.698 < 2e-16 ***
cb4
                                42.790 < 2e-16 ***
cb5
            0.93938
                       0.02195
                                28.028 < 2e-16 ***
cb6
            1.02521
                       0.03658
                                23.391 < 2e-16 ***
cb7
            0.92175
                       0.03941
                                      < 2e-16 ***
cb8
            1.26067
                       0.03405
                                37.022
                                36.963 < 2e-16 ***
ch9
            1.50346
                       0.04067
cb10
            1.54649
                       0.06590 23.466 < 2e-16 ***
(Dispersion parameter for binomial family taken to be 1)
```

Null deviance: 233160 on 205685 degrees of freedom Residual deviance: 205585 on 205633 degrees of freedom

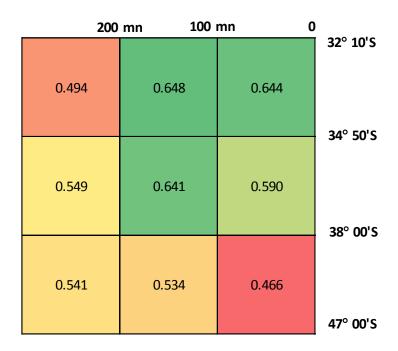


Figure 5. Graphical representation of the area factor in the CPUE model. Green represents highest values and red the lowest values.

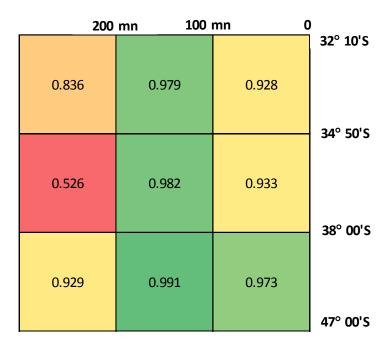


Figure 6. Graphical representation of the area factor in model of catches's success. Green represents highest values and red the lowest values.

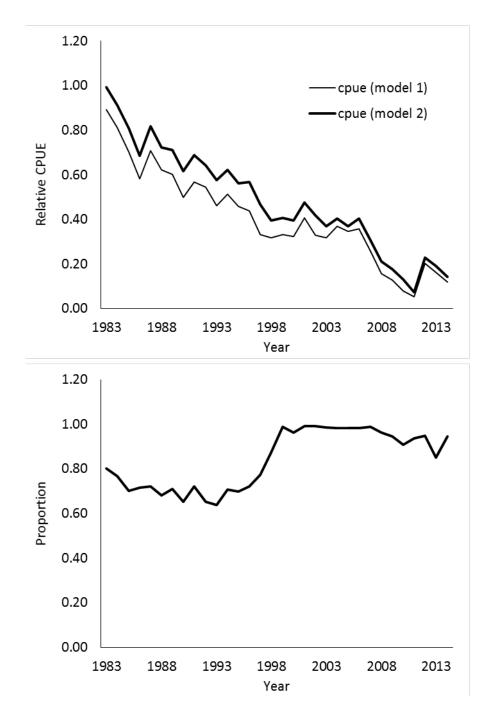


Figure 7. CPUE relative (upper panel) and proportion of days with catch (catch success) (lower panel)

3.3. Abundance index

The combination of models of CPUE and success of catches allowed to estimate an annual abundance index, and showed that the population's reduction had been occurring until the mid 90s (Fig. 8). After a transient stability, in 2006 the population started a new decline until 2011 and reached the lowest value equivalent to 12% of the CPUE recorded in 1983.

The increase of the CPUE occurred in 2012 is the result of an increase in resource availability within the EEZ. Nevertheless, the overall declining trend maintained until the present (i.e. 2014).

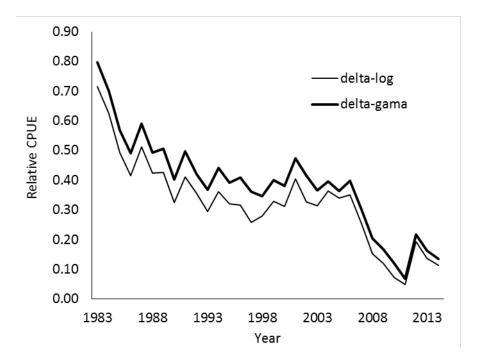


Figure 8. Abundance index of jack mackerel 1983-2014.

4. Discussion

CPUE as abundance index of jack mackerel in the center-south area off Chile was updated. Methodology was similar to that used by Caballero *et al* (2013), who used as effort unit the daily deployment of hold capacity. In this sense, the days out of port represent the deployment of fleet capacities to achieve catches in a better way, and secondly, the hold capacity generates a measure of pre-standardized effort, since it is well known that in purse seiners, the fishing power is proportional to the hold capacity.

The analysis allowed the identification of the spatial patterns in this fishery, observing that the main density of jack mackerel is located north of 38° S and inside the EEZ, while in terms of capture success, the highest scores are recorded between 100 and 200 nm along the entire area of analysis.

Moreover, catch success showed a significant change around 2000-2001 when reached values close to 96% due to adjustments in the fleet at the end of the 90's, and also to the enactment of the Fishing Act (2001) which established the measure known as Maximum Catch per Vessel Owner. This situation determined an important reduction in the number of vessels along with the increase in the fleet efficiency, despite the fact that fishing grounds were located farther and the number of days out of port between 2008 and 2011 increased.

The abundance signal indicates that after a sharp decline until 1998, the jack mackerel stock remained temporarily at stable levels until 2006, and then experienced a significant reduction which maintains to date, although an important change in availability was observed in 2012.

5. Bibliography

Aranis A., L. Caballero, A. Gómez, S. Mora, M. J. Zúñiga, G. Muñoz, L. Ossa, F. Cerna, V. Bocic, C. Machuca, L. Muñoz, C. Vera y G. Eisele. 2011. Informe Final ASIPA "ASESORÍA INTEGRAL PARA LA TOMA DE DECISIONES EN PESCA Y ACUICULTURA 2011, Pesquería Pelágica Centro-Sur. Seguimiento del Estado de Situación de las Principales Pesquerías Nacionales. Subsecretaría de Pesca, Inst. Fom. Pesq. Valparaíso, Chile. 215p + Anexos.

McCullagh, P. and Nelder, J. 1989. Generalized linear models. Chapman and hall. London. 511 pp. Ortiz, M and F. Arocha. 2004. Alternative error distribution models for the standardization of catch rates of non-target species from a pelagic longline fishery: billfish species in the Venezuelan tuna longline fishery. Fisheries Research. 70: 275-297.

Pennington. M. 1983. Efficient estimators of abundance for fish and plankton surveys. Biometrics 39:281-286.

Stefánsson, G. 1996. Analysis of groundfish survey abundance data: combining the glm y delta approaches. Ices Journal of Marine Science, 53: 577 – 588 p.